Limited recharge of the southern highlands aquifer on early Mars

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Highlights

- 1 Highlights
- ² Limited Recharge of the Southern Highlands Aquifer on Early Mars
- ³ Eric Hiatt, Mohammad Afzal Shadab, Sean P.S. Gulick, Timothy A. Goudge, Marc A. Hesse
- Analytic and numerical solutions for an unconfined aquifer beneath Mars' southern highlands provides first-order estimates of groundwater table elevation.
- The key control on the steady groundwater table elevation is the ratio between mean recharge and mean hydraulic conductivity of the aquifer.
- For commonly assumed values of hydraulic conductivity, the steady recharge must be at the lower end of the estimated range of recharge fluxes.

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ABSTRACT

To determine plausible groundwater recharge fluxes on early Mars, we developed analytic and numerical solutions for an unconfined steady-state aquifer beneath the southern highlands. We showed that the aquifer's mean hydraulic conductivity, K, is the primary constraint on the plausible magnitude of the mean steady recharge, r. By using geologic constraints, a mean hydraulic conductivity of $K \sim 10^{-7}$ m/s, and varying shoreline elevations and recharge distributions, the mean recharge must be of the order of 10^{-2} mm/yr. Recharge for other values of K can be estimated as $r \sim 10^{-5} K$. Our recharge value is near the low end of previous estimates and significantly below published precipitation estimates. This suggests that, in a steady hydrologic cycle, most precipitation forms runoff as opposed to infiltrating into the subsurface. Alternatively, high rates of runoff production combined with a sufficiently slow transient aquifer response to recharge may limit major groundwater upwelling prior to the cessation of climatic excursions causing precipitation.

35 1. Introduction

The surface of Mars retains several planetary scale structures. The largest is the crustal dichotomy separating Mars' northern lowlands from its southern highlands via an abrupt ~ 5 km topographic transition (Figure 1). In stark contrast to the smooth plains in the north, the highlands preserve the oldest, most heavily cratered terrain on the planet as well as two large impact basins, Hellas and Argyre (Smith et al., 1999). These structures formed prior to ~3.7 Ga, in the Noachian Era, when Mars is also hypothesized to have had an active hydrologic cycle (Carr, 1986; Clifford, 1993; Frey, 2008; Werner, 2008). The formation of these structures would have impacted any possible surface and groundwater processes due to their associated topographic lows.

There is ample evidence for liquid water on Mars' surface early in the planet's history. The eroded remains of 43 poorly integrated fluvial drainage systems, called "valley networks", dissect the highlands (Milton, 1973; Goldspiel 44 and Squyres, 1991; Carr, 1996; Hynek and Phillips, 2001). Spectral data strengthen inferences of past surface water 45 related processes with observations of hydrated silicates that suggest near surface aqueous mineral alteration (Mustard 46 et al., 2008; Ehlmann et al., 2009; Carter et al., 2013). Open and closed crater lakes have been identified throughout 47 the Noachian terrain, providing further evidence of standing bodies of water on the Martian surface (Cabrol and Grin, 48 1999; Fassett and Head III, 2008; Di Achille and Hynek, 2010). Additionally, observations in Argyre and Hellas also 49 support the possible past existence of large standing bodies of water within these basins (Parker et al., 2000; Wilson 50 et al., 2010; Dohm et al., 2015; Hiesinger and Head, 2002; Hargitai et al., 2018; Zhao et al., 2020). Many have also 51 argued that an immense ocean once existed within the lowlands (e.g., Parker et al., 1989, 1993; Carr and Head, 2003). 52 Evidence of surface water processes and standing bodies of water naturally leads to questions regarding the 53 formation and extent of any groundwater systems. A globally connected groundwater system has been inferred in 54 numerous geomorphic and numerical modeling based studies (e.g., Clifford, 1993; Andrews-Hanna et al., 2007; Di Achille and Hynek, 2010; Salese et al., 2019). Additionally, observations of layered deposits in Arabia Terra 56 (Figure 1) have been interpreted as evaporites resulting from groundwater upwelling (Christensen et al., 2000; 57 Golombek et al., 2003; Squyres et al., 2004; McLennan et al., 2005; Grotzinger et al., 2005; Bibring et al., 2007; 58

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Andrews-Hanna et al., 2007). These findings suggest that Mars had an active groundwater hydrology, but its coupling
 with surface hydrology through groundwater recharge and upwelling is poorly understood.

Here we investigate the plausible values of groundwater recharge as constrained by large-scale topography and geologic observations. The aim of this work is not to constrain the specific hydrology at discrete time periods on early Mars, but to establish constraints on the total rates of groundwater recharge that are plausible given geologic observations. With this aim, we then compare our findings to published estimates of precipitation rates. In doing so, some insight into groundwater-to-surface water coupling may be gained, however this requires simplifying assumptions regarding basin hydraulic head levels, hydraulic conductivity, and recharge distributions.

To examine the effect of standing bodies of water on possible groundwater recharge, we use mean shoreline 67 elevations of Deuteronilus (-3790 m), Arabia (-2090 m), and Meridiani (0 m) as illustrative examples (see Table 1 in 68 Carr and Head (2003) and Figure 1). The existence of a northern ocean remains contentious, with some studies arguing that the kilometer-scale deviation of equipotential shorelines preclude the possibility of any ocean(s) (e.g., Malin and 70 Edgett, 1999; Sholes et al., 2019, 2021; Sholes and Rivera-Hernández, 2022); however, others have suggested that true 71 polar wander and/or deformation associated with the Tharsis Rise can explain these discrepancies (Perron et al., 2007; 72 Citron et al., 2018; Chan et al., 2018). Although each of these individual shorelines is uncertain, together they allow hydrologic models to span a large parameter space in Mars' total water budget. Here, we show that the existence of 74 a northern ocean, regardless of extent, is a secondary control on groundwater when compared to the geometry of the 75 dichotomy. 76



Figure 1: Topography of Mars derived from Mars Orbiter Laser Altimeter (MOLA) aboard the Mars Global Surveyor (MGS) mission (Smith et al., 1999). Hellas and Argyre impact basins are labeled along with the northern lowlands. Three mean shoreline elevations are taken from Parker et al. (1989) and Carr and Head (2003). Argyre and Hellas impact basins are outlined at an elevation of -2090 m.

The distribution of valley networks offers insight into groundwater table elevation, which often sets the local base 77 level to which fluvial systems can erode. The wide distribution of incised valley networks implies that any groundwater 78 table was likely below the surface topography over much of the planet (Hynek et al., 2010). Similarly, Arabia Terra's 79 noticeable lack of incised valley networks and the presence of inverted fluvial channels suggests that the region was a 80 depositional environment, with a groundwater table at or near the surface consistent with rover observations (Squyres 81 et al., 2004; Grotzinger et al., 2005; Davis et al., 2016, 2019). Evidence that the groundwater table was significantly 82 below topography, everywhere except in Arabia Terra, provides a constraint on plausible groundwater recharge fluxes. 83 Published aquifer recharge and precipitation rates vary by orders of magnitude. Estimates of water availability due 84 to snow and ice accumulation give values ranging from 10^{-2} to 10^3 mm/yr (e.g., Wordsworth et al., 2015; Fastook 85 and Head, 2015; von Paris et al., 2015) and estimates of precipitation range of $10^0 - 10^3$ mm/yr (e.g., Kamada et al., 86

⁸⁷ 2020; Wordsworth et al., 2015). Geomorphic studies have estimated water associated with runoff production between ⁸⁸ 10^2 to 10^5 mm/yr (Ramirez et al., 2020; Hoke et al., 2011). However, these studies only provide an upper bound on ⁸⁹ groundwater recharge due to the unknown partitioning between runoff and infiltration.

Direct estimates of recharge from previous modeling studies vary between 10⁻² to 10³ mm/yr, but require the specification of unknown aquifer properties (Harrison and Grimm, 2009; Andrews-Hanna et al., 2007, 2010; Luo et al., 2011; Horvath and Andrews-Hanna, 2017). Here, we examine the importance of these properties individually, the effects of possible standing bodies of water, and consequences associated with varying recharge distributions on the aquifer using novel analytic and numerical groundwater models. By comparing solutions with the inferred depositional environment within Arabia Terra and the distribution of valley networks, we ask: what are plausible mean recharge estimates for a steady-state aquifer on early Mars?

97 2. Methodology

98 2.1. Model for the southern highlands aquifer

Similar to many previous large-scale groundwater studies on Mars (e.g., Clifford, 1993; Hanna and Phillips, 2005; Luo and Howard, 2008), we use the Dupuit-Boussinesq model (Dupuit, 1863; Forchheimer, 1901; Boussinesq, 1903). This approach relies on the large aspect ratio of the aquifer to assume groundwater flows predominantly horizontal. This assumption reduces the dimensionality and computational cost of the model, which makes planetary-scale computations feasible. For a recent review of this approach to large-scale groundwater modeling, with a derivation of the governing equations and an explanation of their physical interpretation, see Troch et al. (2013). At steady state, this model leads to the following non-linear elliptic partial differential equation for the height, *h*, of the groundwater table above the base of the aquifer given by

$$-\nabla \cdot [K \, h \nabla h] = r \, \chi(\theta, \theta_r), \tag{1}$$

where θ is the angle from the south pole or southern colatitude, K is the hydraulic conductivity, r is the recharge, and 107 χ is an indicator function. The divergence and gradient take their standard form in spherical shell coordinates; see 108 SI Section S3.2. For clarity of presentation, we assume that both K and r are constant and hence refer to them as the 109 mean hydraulic conductivity and the mean recharge; however, our numerical computations can be extended to spatially 110 variable conductivity and recharge. Figure 2a shows that the base of the aquifer is assumed to be at an elevation of 111 $z_B = -9$ km, consistent with previous studies (Andrews-Hanna et al., 2010; Andrews-Hanna and Lewis, 2011). For 112 a mean elevation of the highlands of $z_H = 1$ km, the aquifer has a maximum thickness of $d = z_H - z_B = 10$ km, 113 similar to previous work (Hanna and Phillips, 2005). In this reference frame, the elevation of the groundwater table is 114 given by $z_{GW} = z_B + h$. 115

We assume that the recharge, r, is evenly distributed in a latitudinal band of angular width, $\Delta \theta_r = 180^\circ - 2\theta_r$, 116 between the colatitude θ_r and $180^\circ - \theta_r$ (Figure 2b). This band is defined by the indicator function $\chi(\theta, \theta_r)$ that is one 117 for $\theta_r \le \theta \le 180^\circ - \theta_r$ and zero otherwise. We note that the recharge, r, is a *flux*, i.e., a volume per unit area per unit 118 time. The total rate of recharge can be obtained by integrating the flux over the surface area of the aquifer. We assume 119 that groundwater recharge occurs only on land, so that the boundaries of the recharge band may be influenced by the 120 shorelines. This implies that for the same recharge flux, r, and width of recharge band, $\Delta \theta_r$, the total aquifer recharge 121 rate changes for different shore lines. Finally, the recharge should be considered as a temporally averaged quantity, 122 because we consider a steady system. 123

124 2.2. Analytic Solutions for an idealized spherical cap aquifer

To gain a first-order understanding of the groundwater dynamics, we derive analytic solutions in an idealized spherical cap aquifer with azimuthal symmetry. The spherical caps corresponding to the three shorelines shown in Figure 1 are illustrated in Figure 2*c-e*. We choose the southern colatitude of the mean shoreline, θ_0 , so that the surface area of the idealized spherical cap aquifer is equivalent to the area enclosed by the complex shoreline in Figure 1. In this limit, the solution is only a function of latitude, θ and equation (1) reduces to the following differential equation

$$-\frac{1}{R\sin\theta}\frac{\mathrm{d}}{\mathrm{d}\theta}\left[\frac{K}{R}\sin\theta h\frac{\mathrm{d}h}{\mathrm{d}\theta}\right] = r\,\chi(\theta,\theta_r) \quad \text{on} \quad \theta \in \left[0,\,\theta_{\mathrm{o}}\right],\tag{2}$$



Figure 2: Simplified model and analytic solutions. *a*) Cross-section through the one-dimensional azimuthally symmetric Dupuit-Boussinesq model for the southern highlands aquifer. The azimuthally averaged MOLA topography is shown in gray and the simplified step function topography for the Deuteronilus shoreline is shown in black. The groundwater table and sea level are shown in blue. *b*) Construction of the composite solution with a longitudinal recharge band for case 3. *c-e*) Three shorelines from Carr and Head (2003) shown in black together with the equal-area spherical cap aquifer shown in dark gray and the complementary spherical cap ocean in light gray.

where $R \approx 3390$ km is the mean radius of Mars (Smith et al., 1999), and θ_0 is the southern colatitude of the mean shoreline of the northern ocean and *r* is the mean recharge flux. We assumed a simple step in topography at the shoreline, θ_0 , between the mean elevation of the highlands, $z_{\rm H} = 1$ km, and the mean elevation of the lowlands, $z_{\rm L} = -4$ km (Figure 2*d*). At the south pole, the groundwater table is horizontal by symmetry, $dh/d\theta|_{\theta=0} = 0$, and along the shoreline the head is prescribed, $h(\theta_0) = h_0$ (Figure 2*a*).

In particular, we are interested in the effect that the width of the recharge band, $\Delta \theta_r$, has on the groundwater table and plausible recharge fluxes. As the width of the latitudinal recharge band, $\Delta \theta_r$, is varied, three different cases must be distinguished in the analytical solution. The first and simplest case is uniform recharge over the entire aquifer, and the other two cases are for partial recharge.

139 2.2.1. Uniform recharge (Case 1)

In the simplest case, the recharge is uniform across the entire highlands, $\theta_r = 0$ and $\chi(\theta, 0) = 1$. We have presented the analytic solutions for this limiting case in (Shadab et al., 2022). The head is given by

$$h(\theta) = \sqrt{h_o^2 + 2\frac{rR^2}{K} \ln \left| \frac{\cos \theta + 1}{\cos \theta_0 + 1} \right|}, \quad \text{for} \quad \theta \in [0, \, \theta_0] \,, \tag{3}$$

and shown in Figure 2*a*. The solution for case 1 becomes the basis for the analytic solutions with heterogeneous recharge distributions discussed below. Shadab et al. (2022) also shows the associated specific discharge, $q(\theta) = -Kdh/d\theta$, and the discharge $Q(\theta) = h(\theta)l(\theta)q(\theta)$, where $l = 2\pi R \sin \theta$ is the length of the small circle with colatitude θ . Mass/volume balance at steady state requires that the discharge must equal the recharge rate, $Q(\theta) = rA(\theta)$, where $A(\theta) = 2\pi R^2(1 - \cos \theta)$ is the area of the spherical cap. These relations also hold for the other cases given below.

147 2.2.2. Partial recharge

Here, we present new solutions for an unconfined aquifer with partial recharge, $0 < \theta_r < 90^\circ$. In all cases, we assume recharge in a longitudinal band between θ_r and $180^\circ - \theta_r$ of width $\Delta \theta_r = 180^\circ - 2\theta_r$. First, we consider the case where the northern boundary of the precipitation band, $180^\circ - \theta_r$, is north of the dichotomy shoreline, θ_o , that bounds the aquifer (Case 2). Then, we consider the case of a latitudinal precipitation band that is entirely south of the dichotomy shoreline (Case 3). In this latter case, the northern-most part of the aquifer does not receive recharge and flow in this regions is entirely due to lateral inflow from the south.

• Case 2 (180° – $\theta_r \ge \theta_0$): In this case, recharge starts at the most southern colatitude of the recharge band, θ_r , and extends to our chosen ocean shoreline at θ_0 . The solution for the head is piece-wise defined and given by

$$h(\theta) = \begin{cases} h_{\max} = h(\theta_r) = \text{const.}, & 0 \le \theta < \theta_r, \\\\ \sqrt{h_o^2 + 2\frac{rR^2}{K}\Delta(\theta, \theta_r, \theta_o)}, & \theta_r \le \theta \le \theta_o, \end{cases}$$

where we have introduced the geometric function

$$\Delta(\theta, \theta_r, \theta_o) = \ln \left| \frac{\sin \theta}{\sin \theta_o} \right| - \cos \theta_r \ln \left| \frac{(\cos \theta + 1) \sin \theta_o}{(\cos \theta_o + 1) \sin \theta} \right|$$
(5)

- that arises from the integration on the sphere. In the limit of $\theta_r \to 0$ this function reduces the logarithmic term in equation 3.
 - Case 3 ($180^\circ \theta_r < \theta_o$): In this case, recharge starts at θ_r and extends only until $180^\circ \theta_r < \theta_o$, so that the northern most portion of the aquifer does not receive any recharge, r = 0, but a discharge, Q_r , from the region within the latitudinal recharge band. The different elements in the construction of this solution are illustrated in Figure 2b. The solution for the head in the region without a recharge is given by

$$h'(\theta) = \sqrt{h_o^2 + \frac{Q_r}{\pi K} \ln \left| \frac{\tan(\theta_o/2)}{\tan(\theta/2)} \right|}.$$
(6)

The discharge this area receives is the total recharge integrated over the latitudinal recharge band and given by $Q_r = 2\pi R^2 \left(\cos(\theta_r) - \cos(180^\circ - \theta_r)\right) r$. Given Q_r , the head at the northern boundary of the latitudinal recharge band total can be calculated as

$$h_b = h'(180^\circ - \theta_r) = \sqrt{h_o^2 + \frac{Q_r}{\pi K} \ln \left| \frac{\tan(\theta_o/2)}{\tan((180^\circ - \theta_r)/2)} \right|}.$$
(7)

This head forms the boundary condition for the solution within the latitudinal recharge band, which is similar to equation (4) except that h_o is replaced with h_b . The full piece-wise solution for case 3 is then given by

$$h(\theta) = \begin{cases} h_{\max} = h(\theta_r) = \text{const.}, & 0 \le \theta < \theta_r, \\ \sqrt{h_b^2 + 2\frac{rR^2}{K}\Delta(\theta, \theta_r, 180^\circ - \theta_r)}, & \theta_r \le \theta < 180^\circ - \theta_r, \\ h'(\theta) = \sqrt{h_o^2 + \frac{Q_r}{\pi K}\ln\left|\frac{\tan(\theta_o/2)}{\tan(\theta/2)}\right|}, & 180^\circ - \theta_r \le \theta \le \theta_o, \end{cases}$$
(8)

where $\Delta(\theta, \theta_r, 180^\circ - \theta_r)$ is given by equation (5).

The solutions for all three cases, equations (3), (4) and (8), depend only on the dimensionless ratio r/K and not on r and K individually. The physical interpretation of this ratio is that it takes more recharge to sustain the water table at a given height if the regolith is very conductive and allows the water to flow away quickly. Therefore, below we will discuss the plausible recharge values in terms of this ratio.

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Figure 3: Treatment of complex shorelines in the numerical groundwater model. *a*) The global mesh is shown in gray with the Arabia shoreline and the equivalent elevation shorelines in the Hellas and Argyre basins are shown in black. The green outline shows the zoom-in area shown in panels *b* and *c*. *b*) Numerical mesh in the vicinity of the Hellas basin. Active cells are shown by green dots, and inactive cells are shown by red dots. Black dots identify the cells where the boundary condition corresponding to the Hellas shoreline is imposed. *c*) The resulting numerical solution for the groundwater table in the vicinity of the shoreline in the Hellas basin.

2.3. Maximum recharge value

The analytic solutions presented above allow a first-order estimate of the plausible r/K ratio over a wide parameter space. To place constraints on plausible recharge values, we used the observation that the groundwater table was below topography in the majority of the highlands. In our analytic model widespread upwelling would occur if the elevation of the groundwater table exceeds the mean elevation of the highlands, $\max(z_{GW}) = z_H$, see Figure 2*b*. Because the water table is always highest at the south pole this is equivalent to requiring that $h(0) = z_H - z_B = d$. Substituting this into equations (3), (4), (8) and solving for r/K, we obtain the maximum r/K ratio for each case as



These results will be discussed in section 3.

177 2.4. Numerical Model for southern highlands aquifer

To investigate the effects of complex shorelines and basins on plausible recharge fluxes, we developed a numerical model for the highlands' aquifer. We non-dimensionalized equation (1) and discretized it in spherical shell geometry. The model uses conservative finite differences on a tensor product grid with an operator-based implementation (LeVeque, 1992). The resulting non-linear system of equations is solved with the Newton-Raphson method. More details of the numerical model and the benchmark test can be found in SI Section S3. For consistency between the analytic and numerical models all dimensional simulation results use a hydraulic conductivity of, $K = 10^{-7}$ m/s.

To obtain the locations of the shorelines in the northern lowlands and basins, the MOLA topography is downsampled to our grid pixel resolution of 1.2° (Figure 3*a*). Next, these shorelines are used to divide the computational domain into the highlands aquifer and three open water basins by assuming an equipotential surface across a standing body of water. Cells within these basins must be excluded from the computations (Figure 3*b*). We locate the cell faces corresponding to the elevation of the chosen basin, for example the cells marked red within the Hellas basin in

Figure 3*b*. The entries corresponding to inactive cells can be removed from the matrix equation using the projection approach (see Shadab and Hesse, 2022, for details). The reduced matrix system of discrete governing equations can then be solved on the active cells (green dots in Figure 3*b*). The resulting head distribution in the vicinity of the Hellas basin is shown in Figure 3*c*.

When a portion of the specified recharge band extends north of the chosen shoreline, the prescribed recharge flux is not added to the system under the assumption that rainfall in a large body of water has a net zero effect on the water level. As such, the same latitudinal recharge band can lead to different total recharge rates for different shorelines.

3. Results

The analytic and numerical aquifer models provide complementary information about the plausible steady-state recharge values for Mars' highlands aquifer. The analytic solution gives insight into the relationship between recharge and hydraulic conductivity, whereas the numerical results allow us to investigate the effects of complex shoreline geometries. Although the analytic solution is highly simplified, the order of magnitude agreement between both solutions provides confidence between the solutions.

Neither the mean hydraulic conductivity nor the mean recharge of the highlands aquifer are known. Our analysis shows that the solution for the head, given by equations (3, 4, 8), is primarily a function of the dimensionless ratio between recharge and hydraulic conductivity, r/K. This ratio allows us to estimate which recharge values are plausible given any proposed mean hydraulic conductivity. For example, Figures 4a-4c show the elevation of the groundwater table in the spherical cap aquifer for different shorelines and increasing recharge values. For a hydraulic conductivity of 10^{-7} m/s, the analytic model predicts recharge values on the order of 10^{-2} mm/yr are capable of raising the groundwater table to the surface.

Requiring groundwater elevation lower than topography in the majority of the highlands constrains plausible r/K209 ratios. Figure 4d shows the plausible combinations of hydraulic conductivity and recharge for the Arabia shoreline. 210 This illustrates that reducing the mean K by an order of magnitude requires a similar drop in the mean r to prevent 211 widespread upwelling. The effects of varying other parameters, such as the chosen shoreline (Figure 4a-4c) or the 212 recharge distribution (Figure 4e-4g) are less than an order magnitude. For example, if the width of the recharge band, 213 $\Delta \theta_r$, is varied by $\pm 20^\circ$ around the preferred value of 90° for an aquifer with $K = 10^{-7}$ m/s the maximum plausible 214 values of the mean recharge for the three shorelines vary only between $6 \cdot 10^{-3}$ and $1.6 \cdot 10^{-2}$ mm/yr (Figure 4*h*). The 215 analytic model already demonstrates that the recharge estimates are not very sensitive to the recharge distribution. The 216 numerical results below show that this is even less important when complex shorelines are present. In that case, the 217 hydraulic head level is more sensitive to the distance to the shoreline than it is to the recharge distribution. 218

Analysis of the simplified spherical cap aquifer model demonstrates that the elevation of the groundwater table is primarily a function of the r/K ratio. Although the mean K of the southern highlands is not known, reasonable values in the range of 10^{-6} to 10^{-8} m/s (Hanna and Phillips, 2005) require very low groundwater recharge rates to avoid widespread groundwater upwelling (Figure 4*d*). This conclusion is relatively insensitive to the particular shoreline chosen, the latitudinal width of the precipitation band, or the depth of the aquifer base. The particular value of the ratio r/K is primarily determined by the large surface area of the highlands relative to the cross-sectional area of the aquifer, as discussed in Section 4.

To explore the effect of complex shorelines, we present numerical solutions using the Arabia shoreline, $K = 10^{-7}$ 226 m/s, and $r = 10^{-2}$ mm/yr (Figure 5). First, we explore the effect of the shoreline alone and then consider the influence 227 of adding the Hellas and Argyre basins. When comparing the analytic solution for the spherical cap aquifer (Figure 5a) 228 with the numerical solution for the Arabia shoreline (Figure 5b), we observe an overall drop in the elevation of the 229 groundwater table. The complex shoreline generates a local maximum in groundwater elevation at the farthest location from a shoreline within the precipitation band. The complex shoreline has an increased shoreline length and reduces 231 the distance to drain into a basin resulting in more effective drainage. The presence of basins further lowers the head 232 in the aquifer (Figure 5c). These basins provide additional shorelines within the highlands that help drain the aquifer. 233 Results for other shorelines are provided in the SI Section S4.3 and S4.4. 234

Overall, our numerical model demonstrates that complex shorelines lower the head in the aquifer and therefore increase the plausible value of mean recharge. However, these geometric effects do not change the order of magnitude of the plausible range for r/K. As such, the unknown mean hydraulic conductivity of the highlands remains the dominant control on the allowable mean recharge. In Figure 6, we explore the location and extent of groundwater upwelling in the highlands as a function of mean recharge in an aquifer bounded by the Arabia shoreline at the dichotomy and



Figure 4: *a-c*) Analytic solution for steady unconfined aquifer on a spherical shell. Elevation of the groundwater table for the mean elevations of the Meridiani, Arabia, and Deuteronilus shorelines of Carr and Head, 2003. In each case, the groundwater table is shown for multiple recharge values, as given by the legend in panel *b. d*) Depth of groundwater beneath mean highland elevation, $z_{\rm H} = 1$ km for the Arabia shoreline. The parameters corresponding to the solutions from panel *b*) are plotted as dots. The maximum plausible recharge from equation (9) is shown in red. Note that these solutions assume that recharge extends to the shoreline, $\theta_o \leq 180^\circ - \theta_r$. *e-g*) The Deuteronilus shoreline is utilized to examine the effect of recharge distribution. The region receiving recharge is varied and shaded in shaded blue. The recharge color scheme, used in *a-c*, remains. *h*) The effect of the thickness of the recharge band on the maximum recharge flux is examined. Note that the hydraulic conductivity remains constant at $K = 10^{-7}$ m/s and the x-axis is the total width of recharge above and below the equator. The gray line in the elevation plots refers to the azimuthally averaged MOLA topography.

shorelines of equivalent elevation in Hellas and Argyre. Figure 6a-6c shows the depth, compared to topography, of the groundwater table for a succession of simulations with increasing amounts of recharge. Areas with deep blue colors are submerged, whereas areas of groundwater upwelling are shown in white and light blue regions. For $r = 10^{-2}$ mm/yr the highlands do not experience significant upwelling outside of some deep craters (Figure 6a), suggesting r is too low. Increasing the recharge to $3 \cdot 10^{-2}$ mm/yr forms a region of groundwater upwelling in Arabia Terra (Figure 6b), where geologic observations suggest upwelling has occurred (e.g., McLennan et al., 2005; Grotzinger et al., 2005;



Figure 5: Effect of complex geometry for an aquifer with a recharge flux of 10^{-2} mm/yr evenly distributed between -45° and 45°: *a*) Analytic solution from equation 4 with mean Arabia shoreline. *b*) Numerical solution with Arabia shoreline *c*) Numerical solution with Arabia shoreline and standing water in Hellas and Argyre basins. The hydraulic head level in the basins is assumed to be equal to the Arabia shoreline elevation. All numerical solutions presented in this work assume a hydraulic conductivity of $K = 10^{-7}$ m/s and assume that all basins have shoreline elevations equivalent to the Arabia Terra shoreline at -2090 m. Results for other shorelines are provided in the SI Section S4.3 and S4.4.

Davis et al., 2016, 2019). A further increase in recharge to only 10^{-1} mm/yr results in large areas of the highlands experiencing upwelling beyond that supported by observations (Figure 6*c*).

The area of the highlands that experiences groundwater upwelling grows rapidly with increasing recharge 248 (Figure 6d). Therefore, the lack of evidence for pervasive depositional environments in the highlands places a constraint 249 on the plausible r/K ratio. For the mean hydraulic conductivity $K = 10^{-7}$ m/s, the recharge that best reproduces the 250 observed geology qualitatively is approximately $3 \cdot 10^{-2}$ mm / year, leading to 6.3% of the highlands experiencing 251 upwelling (Figure 6b). This solution is obtained using a fairly large recharge band from -45° to 45° , however, the 252 numeric model is less sensitive to recharge distribution than the analytic model. This is due to the irregular geometry 253 of the shoreline and shortened travel paths to standing bodies of water such as Argyre and Hellas basins as well as 254 Valles Marineris. If the recharge band is reduced to -30° to 30° , the same 6.3% upwelling is observed with only 255 5μ m/yr additional recharge. The calculated r/K remains on the order of ~ 10^{-5} . This is insensitive to any reasonable 256

assumptions regarding recharge distribution and therefore can be used to estimate plausible values of r for any preferred value of K.

4. Discussion

Our results show that a groundwater aquifer beneath the highlands requires very low recharge values to avoid 260 groundwater upwelling occurring outside areas suggested by observational evidence. We show that the plausible 261 steady-state recharge increases linearly with the assumed mean hydraulic conductivity of the aquifer. As such, plausible recharge values for any preferred hydraulic conductivity can be estimated as $r \sim 10^{-5} K$. This relationship is evident 263 from the analytic solutions (equation 8) and confirmed by numerical models of varying complexity. Whereas the 264 geometry of the shorelines has a small effect on the overall magnitude of recharge, Mars' planetary scale topography 265 requires upwelling to occur first in Arabia Terra as recharge increases, in agreement with previous work (Andrews-266 Hanna et al., 2007). If groundwater is assumed to be at or near the surface primarily in Arabia Terra and the chosen K 267 value is held constant, the range of plausible recharge fluxes varies by less than one order of magnitude (Figure 6d). 268 This is consequential because physically informed hydraulic conductivity estimates can be made. Here, we employed 269 a value that is commonly used in Mars groundwater studies (Hanna and Phillips, 2005; Andrews-Hanna et al., 2010; 270 Horvath and Andrews-Hanna, 2017). 271

Previous global groundwater studies estimate recharge fluxes from ~ 10^{-2} mm/yr (Andrews-Hanna et al., 2007) to 272 ~ 10^{-1} m/yr (Andrews-Hanna and Lewis, 2011) for comparable mean hydraulic conductivities, see SI Section S4.1. 273 These estimates are consistent with our results and suggest that they are not strongly dependent on model assumptions. 274 This provides confidence in our methods, given that our model is fundamentally different from any previously published global-scale Martian groundwater model. In previous work, there were no numerical mechanisms to create a complex domain that allowed for standing water and resultant shorelines. Any water that breached the topography was assumed 277 to evaporate and then redistributed across the recharge band (Andrews-Hanna et al., 2007). In doing so, choosing the 278 initial level of the hydraulic head determines the hydraulic head gradients, and the initial hydraulic head gradients 279 control groundwater flux rates out of topographically low areas. The recharge then becomes a dynamic variable of 280 the initial condition rather than an independent parameter space. This modeling method also creates a model that 281 will iterate to steady state unless some method of perturbation is evoked, such as secular water loss. Previous global 282 scale models are essentially the extreme end member of this work in which there is no standing water. Despite all the 283 differences in the model methods and parameterizations, the estimated steady recharge fluxes predicted by previous 284 global models that do not include standing water is 0.01 mm/yr while our model prediction is ~ 0.03 mm/yr (Figure 285 (6b)286

We suggest that low values of acceptable mean recharge are due to the large surface area, A_s , of the aquifer relative to its small cross-sectional area, A_x . This geometric control can be understood by a volume balance over a spherical cap aquifer at steady state. The total rate of recharge is $Q_r = A_s r$ and the total discharge out of the aquifer is $Q_d = A_x q_{\theta}$, where q_{θ} is volumetric flux from Darcy's law. Total volume balance requires that $Q_d = Q_r$, so that

$$\frac{r}{K} = \frac{A_x}{A_s} q_\theta \sim \frac{d\Delta h}{R^2} \sim 10^{-5},$$
(10)

where $R \sim 10^6$ m is the radius of Mars, $d \sim 10^4 m$ is the thickness of the aquifer and $\Delta h \sim 10^3$ m is the elevation change of the groundwater table across the aquifer. Here, we have approximated $A_s \sim R^2$ and $A_x \sim R$ and Darcy's law as $q_{\theta} \sim K\Delta h/R$. This simple estimate is identical to the r/K ratio obtained from the analytic solution and computed from the numerical models (see SI Section S1). It is noteworthy that four methods produced equivalent r/K values. The simple back of the envelope calculation in equation 10, the analytic solutions in equation 9, our complex numerical model, and previous work by Andrews-Hanna et al. (2007;2010, Appendix C) produce nearly identical results.

Although previous work has computed specific recharge values for specific model parameters, our contribution demonstrates the linear relation between r and K that allows estimates of plausible steady recharge for any assumed value of K. This is valuable precisely because K is highly uncertain and the linear relationship allows for the investigation of different scenarios. For example, consider a steady hydrologic cycle in which a significant fraction of precipitation infiltrates and recharges the aquifer. To align with published precipitation estimates, it would require an increase in our model's recharge by nearly two orders of magnitude (Figure 6*d*). The linear relation between rand K would thus require a two order of magnitude increase in the mean conductivity of the aquifer to keep upwelling



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restricted to Arabia Terra. This would require the entire 10 km thick aquifer to have the conductivity of karstic limestone (Freeze and Cherry, 1977).

While local variations in K by several orders of magnitude are not unusual, the K in our equations is the average over the entire aquifer. This average includes rapid decay of the conductivity with depth (Shadab et al., 2023). As such, it is unlikely that the mean K of the aquifer could increase to the value of 10^{-5} m/s, required to make the recharge

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comparable with precipitation estimates of more than 1 mm/yr. If conductivity is lower than assumed here and in previous work (Clifford, 1993; Clifford and Parker, 2001; Hanna and Phillips, 2005), the r/K-relation requires that groundwater recharge in a steady hydrologic cycle is orders of magnitude less than published precipitation estimates (Kamada et al., 2020; Wordsworth et al., 2015). It should be noted that the precipitation estimates are spatially variable. Our work represents both spatially and temporally averaged rates, and this may result in higher recharge values locally. However, the order of magnitude difference between the precipitation estimates and groundwater recharge can only be explained by a few possible mechanisms.

All of the above considerations assume a steady hydrological system because the model presented is at steady state. However, Mars' hydrological activity is believed to occur during short climatic excursions that produce favorable conditions for precipitation (Grotzinger et al., 2014; Wordsworth et al., 2015; Stucky de Quay et al., 2021). In this context, our recharge estimates should be interpreted as average over hydrologically active and inactive periods. As such, the recharge during active periods would almost certainly exceed steady-state values. The large discrepancy between the steady-state recharge fluxes found here and published estimates of precipitation can likely be explained by a combination of several processes.

The simplest way to explain the order-of-magnitude discrepancy between the published precipitation estimates and this work is that both are correct. This would require most precipitation to form runoff rather than recharge the highlands aquifer. It is likely that a combination of a run-off driven system and a delayed transient aquifer response to recharge is the most likely scenario capable of producing published precipitation estimates with low enough recharge fluxes to produced the observed geology.

The transient response of the groundwater table to individual ephemeral precipitation events would depend on the depth of the groundwater table below topography when the recharge event begins, as well as the duration and intensity of recharge. If the transient response time of the aquifer to rise and breach topography is longer than the timescale of climate excursions producing higher recharge values, the groundwater table may not breach the surface before the excursion ends and the recharge declines. The transient aquifer response will be examined in future work and will have implications for constraining the intensity and longevity of climatic events capable of producing recharge.

Lastly, another consideration would be Mars' total water budget. If the Mars GEL (global equivalent layer) were sufficiently low, the evaporative loss would deplete the sources of precipitation and prevent recharge from continuing. In our model simulations with the Arabia Terra shoreline and our preferred recharge value of $3 \cdot 10^{-2}$ mm/yr, the total volume of water contained in the Mars southern highlands aquifer is ~ 670 m GEL, see SI Section S4.2 for calculation. This is a median value compared to values in the literature that range from 100 to 1500 m (e.g., Scheller et al., 2021). However, if there was a significantly limited water budget or a substantial portion of the GEL was not involved in subsurface-surface-atmosphere exchange during the hydrologically active period, a lack of available water as a precipitation source could limit recharge.

Future work will focus on the transient response of groundwater table as well as the conditions required for groundwater connection between the large basins. Each work will require modeling with a dynamic domain for which the algorithm was created in this work. As ocean and basin shorelines move in response to climatically forced evaporation and precipitation, these groundwater-topography interactions must be accounted for. To do so, the governing equation must be modified, and this requires an estimate of r/K (Bresciani et al., 2014, 2016).

5. Conclusions

Our analytical and numerical solutions for the Martian highlands aquifer show that the elevation of the groundwater 348 table is controlled by the ratio of the mean recharge to the mean hydraulic conductivity of the aquifer. This ratio is a 340 function of the geometry associated with the planetary dichotomy. It has implications for constraining the early Martian climate because it allows for estimates of plausible recharge fluxes given any preferred values for aquifer conductivity. 351 For commonly assumed conductivities of ~ 10^{-7} m/s (permeability ~ 10^{-14} m²) the mean groundwater recharge 352 on the highlands is ~ 10^{-2} mm/yr. This value is at the low end of previously proposed estimates and two orders 353 of magnitude below estimates of precipitation. If the hydrologic cycle is at steady-state and published precipitation 354 estimates are correct, then our groundwater models imply that some combination of three possible factors can create 355 low recharge with higher values of precipitation. These possibilities include that most precipitation forms runoff, the 356 transient response of the aquifer to recharge is sufficiently slow that widespread upwelling did not occur prior to the 357 358 cessation of the recharge event, and/or the total water available as surface sources of precipitation are exhausted prior to widespread upwelling. 359

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Declaration of interests

 \boxtimes The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

